

Figure 3 shows a carrier-in-carrier's IC, and consists of a phase-locked loop (PLL) and a delay-locked loop (DLL). With zero frequency offset, and the IC's phase corrections disabled, the overall phase detector's output phase variance, $\sigma_{\Delta\theta}^2$, is the sum of the satellite loop's PN variance, the phase error variance due to thermal noise and in-band interference.

Without oscillator PN, a PLL $\hat{\theta}(n) = \theta(n) - \sum_{k=1}^N h(k)\hat{\theta}(n-k)$ (B_L is the bandwidth of $H(e^{j\omega}) = \sum_{k=1}^N h(k)e^{-j\omega k}$ for phase detection rate f_s and $\omega=2\pi f/f_s$) has phase variance (pg. 128 of [5]), σ_0^2 ,

$$\sigma_0^2 = [(N_0 + I_0)B_L/P^2] \cdot [P + (N_0 + I_0)B_L] \quad (1)$$

P is signal power, while N_0 and I_0 are noise and interference power spectral densities. A digital phase detector requires complex multiplication and low-pass filtering, followed by 4-quadrant arctangent computation. To minimize computations, the phase detector's input rate is reduced (by low-pass filtering and decimation by M , i.e., a *block phase estimator*) as in Figure 3, possibly (depending on the carrier's spectral occupancy) reducing $P=C/M$ (C is outbound carrier power).

Example: For $E_s/(N_0+I_0)=-10$ dB, $M=2$, post-multiplication filtering/decimation at minimum signal bandwidth, BW_{min} , $N=128$, $B_L=BW_{min}/(N \cdot M)$, $P/(N_0+I_0)=14$ dB, thermal-noise induced PN is 0.0414 rad^2 (or 0.2035 rad rms). Demodulator performance is unaffected at moderate bit rates as the PN is low-pass. The approximate mean time to cycle slips (pp. 95 of [5]) is (for small closed-loop phase deviations' variance, $\sigma_{\Delta\theta}^2$) $[\pi/(2B_L)] \cdot e^{(2\sigma_{\Delta\theta}^2)} \approx 3 \times 10^{18} \text{ s}$ ($\sim 3.4 \times 10^{13}$ days).

A unity dc gain, B_L -bandwidth, loop filter, with closed loop response $(1-z^{-1})/\{1-z^{-1} \cdot [H(z)-1]\}$ and lag $\sim B_L^{-1}$, tracks low-frequency ($<B_L$) PN and satellite acceleration³ (high frequency, $>B_L$, PN remaining unaltered). $\sigma_{\Delta\theta}^2$, the IC's output PN is $E[(1-\cos \Delta\theta)^2 + \sin^2 \Delta\theta] = E[2 \cdot (1-\cos \Delta\theta)] \approx E[\Delta\theta^2] = \sigma_{\Delta\theta}^2$, i.e., by Parseval's relation, the integral of the PN's PSD $> B_L$.

Other IC considerations are DLL time resolution (depending on span, L , of a least-mean square adaptive finite impulse response filter, with input sampling rate consistent with cancellation bandwidth⁴) and its noise multiplication (noise

³ For $\pm 0.1^\circ$ N-S and E-W station-keeping, a geostationary satellite's maximum earth station relative velocity is 4m/s and maximum (stabilization-dependent) acceleration of 0.075 m/s^2 [6], i.e., 20ns/s and 4Hz/s delay and frequency change rate at Ku-band; thus, 2 NCO updates/s at an open loop bandwidth of 2Hz, tracks 4Hz/s. Extreme ranges are $R_{min} = [R_e^2 + (R_o + R_e)^2 - 2R_e(R_o + R_e)\cos(\theta-i)\cos\phi]^{1/2}$ and $R_{max} = [R_e^2 + (R_o + R_e)^2 + 2R_e(R_o + R_e)\cos(\theta+i)\cos\phi]^{1/2}$, θ =latitude of earth station, ϕ =satellite longitudinal shift, i =inclination; delay varies by $2 \cdot (R_{max} - R_{min})/c \approx 4[R_e(R_o + R_e)\cos\phi \sin\theta \sin i] / \{c \cdot [R_e^2 + (R_o + R_e)^2]^{1/2}\}$ ($=127 \mu\text{s}$ for $i=0.1^\circ$, $\theta=60^\circ$, $\phi=0^\circ$, $R_o=35,786 \text{ km}$ and $R_e=6,378 \text{ km}$).

⁴ An L -tap DLL converges to a windowed $\text{sinc}[\alpha(n-D)]$, α being the signal's spectral occupancy. L is such that windowing power loss is less than desired IC (e.g., IC=-35dB, $\alpha=1/5$, $L \sim 45$); given L , smaller α degrades IC (also, the signal's autocorrelation matrix's eigenvalue spread, i.e., $\lambda_{max}/\lambda_{min}$, increases, slowing convergence [7]).

variance multiplied by $1+\mu L$ for a unit variance reference, μ being the adaptation step-size [7]). Desired IC determines L , while allowed remote carrier E_b/N_0 degradation (assuming negligible residual outbound carrier) determines μ . A small μ , while reducing noise multiplication, slows DLL response time - system PN must be less than desired IC at its inverse.

Example: IC of -30dB (0.3dB E_b/N_0 degradation at 64kHz cancellation bandwidth) requires DLL lag (B_L^{-1}) of 125ms (i.e., 8000 samples); consequently, the PN at 8Hz should be -27dBc/Hz (approximating the area beyond 8Hz by the area of a triangle (over-estimating the actual integral); the mask value at 8Hz as per IESS-316 is -40dBc/Hz [8] in Figure 4, while the mask value as per IESS-308 is -28dBc/Hz). As seen by the hub's remote carrier's demodulator, the IC further adds to the satellite loop's PN at low frequencies ($<B_L$), with diminishing contribution as frequency is increased (as remote terminal's up-converter PN dominates remote-to-hub PN with no IC).

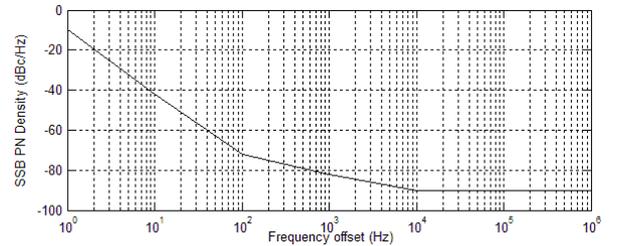


Figure 4: IESS-316 PN mask

In the case of a geostationary satellite, the DLL has a much longer time constant than the PLL (delay rate being small and carrier frequency independent, while Doppler rate increasing linearly with carrier frequency); the two loops don't interact with each other. When a geosynchronous satellite has significant orbital inclination, required Doppler and delay tracking rates are much higher (with maxima at equatorial and high latitudes respectively). This has two consequences:

- Increasing μ to obtain higher DLL tracking rates increases noise multiplication (and hence post-cancellation remote demodulator E_b/N_0 degradation)
- Interacting DLL and PLL increase post-cancellation remote carrier's PN ($<B_L$) and symbol timing jitter.

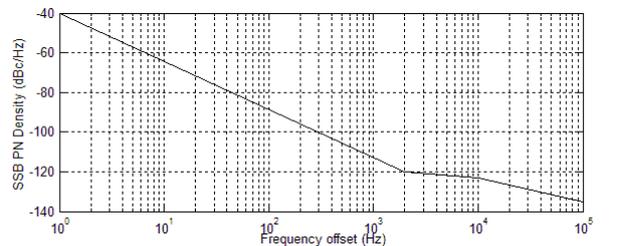


Figure 5: PN mask of sampling clock (here 210MHz)

For a geostationary satellite, the earth-station location and satellite longitude dependent round trip delay, D , is 230-290ms. With both same and different sources (Figure 3's LOs) the reference signal, delayed by D , is time and phase compared (as in Figure 3) with the satellite signal. Therefore, the sampling clock's oscillator PN at $1/D$ must be lower than desired IC. Figure 5 shows a sampling oscillator's PN mask, meeting IC=-30dB at 70 MHz IF and 25MHz bandwidth.

III. DIVERSITY COMBINING

A small aperture terminal, with small angular attenuation over inter-satellite spacing, may utilize adjacent satellites bandwidth to provide a stronger hub⁵ demodulator signal (Figure 6, a weighted addition augmentation of Figure 3's IC). The hub's receive antennas have high directivity (so that they each obtain the spatially separated transponder signals).

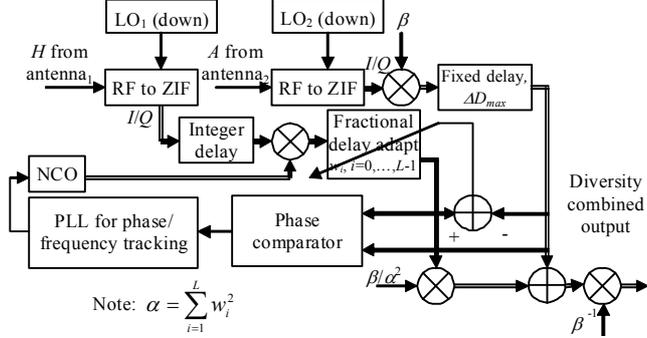


Figure 6: 2-channel (satellites/ hub antennas) MRRC

The range R of a geostationary satellite from an earth station at latitude, θ , and longitudinal shift (from satellite longitude), ϕ , is $R = [R_e^2 + (R_o + R_e)^2 - 2R_e \cdot (R_o + R_e) \cdot \cos\theta \cos\phi]^{1/2}$, $R_o = 35,786\text{km}$ and $R_e = 6,378\text{km}$ [6]. For two satellites' angular separation of (small, typically $2-3^\circ$) $\Delta\phi$, the range difference between hub and satellites $\Delta R \approx 2[R_e(R_o + R_e) \sin\phi \sin\Delta\phi \cos\theta] / [R_e^2 + (R_o + R_e)^2]^{1/2}$, and is maximized when an equatorial earth station has large ϕ (not the best choice as $\phi=0$ maximizes coverage area). The sensor-to-hub range difference, the sum of sensor-to satellite and satellite-to-hub range differences, is maximized when both sensor and hub have the same longitude direction (say ϕ_s and ϕ_h respectively and for farthest sensors, $\phi_s > \phi_h$) relative to the satellite. *Example:* for equatorial sensor and earth station with $\phi_s = 30^\circ$, $\phi_h = 15^\circ$ and $\Delta\phi = 3^\circ$, range differences⁶ are 330 and 171km (1.7ms differential delay).

By design, the two hub receive antennas can have identical apertures; each received signal's strength is sensor location (i.e., relative ratio being the inverse square of the distances to the two satellites) and fading dependent. For two C-band geostationary transponders, this ratio is close to unity (unless the footprints are very different). For equal receivers' noise variances, Figure 6's maximal-ratio receive combining (MRRC) is optimum. Challenges for DC (vis-à-vis IC) are:

- The remote terminal's up-converter's PN is system PN.

⁵ When adjacent satellites have different polarizations and the reduced aperture (e.g., maritime) VSAT's reflector antenna (with bore-sight bisecting the satellites) has receivers at both polarizations [9], forward channel space-polarization-time coding may be used.

⁶ Rapid ionospheric changes at dusk (when total electron content, TEC, drops) induces range differential range $\Delta s = \pm 40.31 \cdot \Delta \text{TEC} / f^2$ m [10], where f is frequency and ΔTEC = differential TEC in m^3 (TEC varies from 1×10^{16} at night to 5×10^{17} at daytime) over the angular inter-satellite separation. Although differential delay uncertainty becomes significant at a sufficiently high symbol rate (or at a low enough carrier frequency), it is negligible at the symbol rate and carrier frequency used in this (sensor data collection) application.

- System bandwidths are typically small (of the order of 0.6-20kHz) because of:

- Many distributed sensors in the satellite's footprint
- Limited remote terminal transmit power

The delay locked loop's lag is reduced (i.e., by increasing μ and decreasing L), compromising diversity gain.

Example: Figure 7(a) shows a low-cost up-converter's PN mask. With 0.1s delay-lock loop time-constant, IC is -17dB (noise multiplication and delay-locked loop time constant being inversely related). Separately, $B_L = 10\text{Hz}$ limits IC to -20dB. With both contributions, IC is -16dB. As predicted, Figure 7(b) has 2.6dB two-satellite MRRC gain (BPSK at 64 ksym/s). In addition, the ratio of combined signal power to PN variance below 10Hz also decreases by 0.4dB (for B_L loop filter, the 2 PN's sum coherently below B_L , but not above B_L).

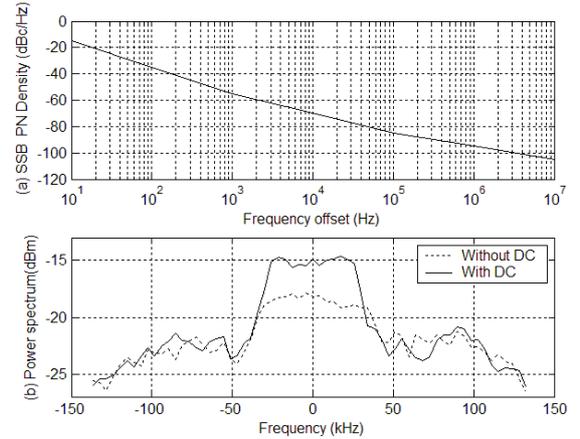


Figure 7: DC gain (b) with low-cost up-converter's PN (a)

IV. AIRBORNE KINEMATIC POSITIONING FOR UAVS

Using the Global Positioning System (GPS), precise airborne positioning via carrier phase measurements has difficulties of:

- Disambiguation
- Cycle slip repair
- Interpolating GPS fixes using inertial navigation

UAVs using low-cost, noisy, surface micro-machined MEMS inertial sensors have significant position and velocity errors. In addition, integrating autonomous target acquisition and bearing-based pursuit⁷ (e.g., phased-array radar in the UAV's nose), is challenging in terms of operating frequency, electronics packaging and cost. Instead, cooperating entities' radio proximity detection (RPD) allows bearing inference.

⁷ Rate-using true proportional navigation guidance [11] may apply (augmented by inter-communicated periodic GPS fixes). Our inherently secure (the target can't separate the two signals without a reference), low probability of intercept (LPI) and anti-jam (AJ) communications method also provides low latency range and Doppler data. Lower the carrier frequency, the smaller the Doppler tracking rate; [12] uses 902-928MHz, which, with 2 carriers, has <3m range resolution, and required Doppler acquisition and tracking of $\pm 2,500\text{Hz}$ (accounting for oscillator offsets and drift) and $\pm 300\text{Hz/s}$ at 700m/s speed and 100m/s^2 acceleration respectively. Short-range (<2km) acquisition, at the signal's sampling rate, suffices in this case (unlike in satellite IC).

Figure 8's "paired-carrier"⁸ RPDs are (i) coordinated UAV pair and (ii) star-coordinated UAVs (using either several paired-carriers or CDMA on a single carrier pair).

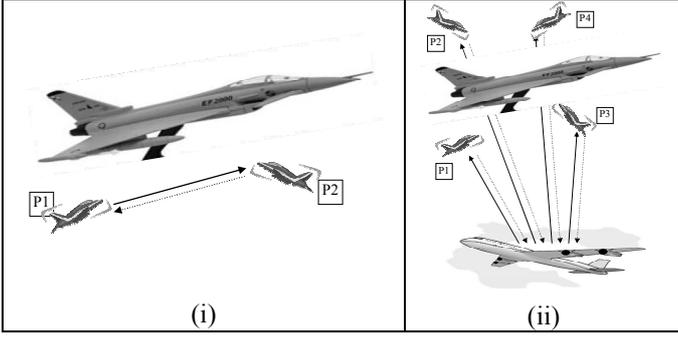


Figure 8: (i) Co-ordinated UAV pair and (ii) UAV swarm

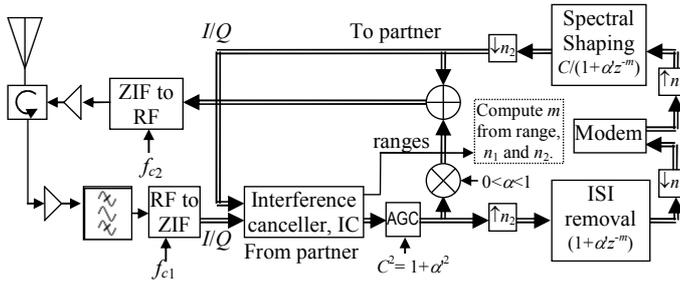


Figure 9: UAV's transceiver⁹; IC cancels all lagged CSs.

In case (i), communication¹⁰ with a partner UAV (each transmitting a different carrier as in Figure 9, with modulator output and α -scaled post-IC received signal termed as communications, CS, and ranging, RS, signals) exploits range and Doppler information inherent in carrier-in-carrier IC. As the target nears, three RS's¹¹ correlate at range lags¹² (in addition to transponder processing lag) of:

⁸ Continuous (rather than pulsed) waveform and a single transmit/receive (T/R) antenna (rather than spatially isolated T/R antennas).

⁹ Low-power, small-footprint, COTS devices spanning 0.8-2.7GHz convert from (to) radio frequency (RF) to (from) zero-IF (ZIF).

¹⁰ Communication signals, with low autocorrelation at non-zero lags (from 0 to 3 times the maximum range lag), modulations may have different discrete amplitude levels [13].

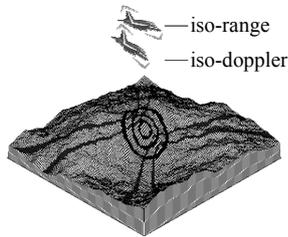
¹¹ Assumes slowly-varying target [14] (where return's amplitude/Doppler can be tracked) and ignores clutter (assumes high-altitude).

Only distant ranges (relative to the target) are received when antenna pattern has high attenuation in a cone about the UAV's downward vertical axis. For typical clutter, the bi-static iso-ranges are incoherent and iso-dopplers time-dispersed. Hence, clutter is modeled as noise (signal being a nearer compact target).

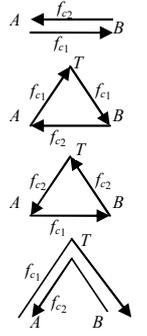
Different UAV's transmit/receive frequencies ensure that only the other UAV's transponder (not its RCS) provide inter-UAV range.

¹² Drawbacks of a system without IC (i.e., 2 carriers for A's communication and B's ranging transponder and, vice-versa, 2 more carriers), besides doubling bandwidth, are:

- The target correlates A's modulator and B's transponder signals to passively obtain (ignoring UAV RCS) lags corresponding to



- Twice the inter-UAV range; receiver power $\propto \alpha^2/(4\pi AB^2)$
- The perimeter of the triangle formed by the two UAVs and the target (whose bi-static radar cross section, RCS, denoted by σ); power $\propto 2\alpha^2\sigma/[(4\pi AT \cdot BT)^2]$ (1-13 of [14], with two ways¹³ of constructing the triangle and $f_{c1} \approx f_{c2}$, $\sigma \gg \lambda^2 = c \cdot f_c^{-1}$).
- Twice the UAVs to target ranges' sum; power $\propto \alpha^2 \cdot AB^2 \cdot \sigma^2 / [(4\pi)^3 (AT \cdot BT)^4]$



Practically, only the first two signals' ICs are relevant and the second return to CS power ratio, $2\alpha^2\sigma(AB)^2/[4\pi(AT \cdot BT)^2]$, sets required IC, (designed to be $>K$, for reliable acquisition).

e 's are unit variance i.i.d. random processes

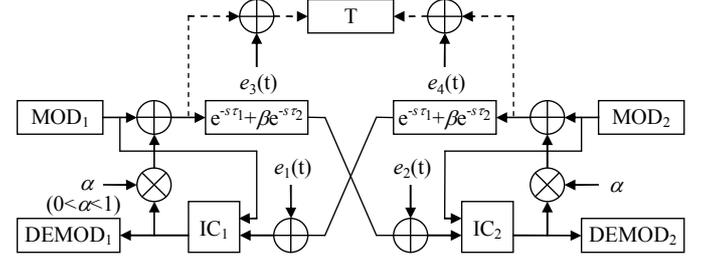


Figure 10: UAV signals' flow graph (no frequency offsets¹⁴)

Figure 10 shows the two UAVs transponders' un-cancelled noise (including jamming and un-cancelled clutter, neglecting CS target path) feedback, including target returns (for LPI analysis, dashed lines showing target's receptions at f_1 and f_2). With fixed delays, noise (as well as un-cancelled signal) amplification (Figure 11) occurs. The input noise spectrum at the left demodulator, $G(s)$, is:

$$G(s) = \frac{(1 + \beta - \alpha\beta e^{-2s\tau_1} - \alpha e^{-2s\tau_2}) [E_1(s) + \alpha E_2(s)]}{(1 - \alpha e^{-2s\tau_1}) \cdot (1 - \alpha e^{-2s\tau_2})} \quad (2)$$

The pass-band noise power gain ($\geq 1 \forall \omega$) is:

$$G(\omega, \alpha, \beta, \tau_1, \tau_2) = \frac{|1 + \beta - \alpha\beta e^{-2j\omega\tau_1} - \alpha e^{-2j\omega\tau_2}|^2 (1 + \alpha^2)}{|1 - \alpha e^{-2j\omega\tau_1}|^2 \cdot |1 - \alpha e^{-2j\omega\tau_2}|^2} \quad (3)$$

$$\bar{G} = G(\alpha, \beta, \tau_1, \tau_2) = \frac{2\pi F_p}{0} \int G(\omega) d\omega \quad (4)$$

Here, $F_p = \text{LCM}(\frac{1}{2}\tau_1^{-1}, \frac{1}{2}\tau_2^{-1})$ Hz, ω is angular frequency and β is target scattering relative to the direct inter-UAV signal. The ratio of UAV-to-target demodulators' signal-to-noise ratios is $\{1 + [\alpha^2 S/G(\alpha, \beta, \tau_1, \tau_2)]\}$; thus, the LPI optimum α is:

$$\alpha_{LPI} = 2G(\alpha, \beta, \tau_1, \tau_2) / [\partial G(\alpha, \beta, \tau_1, \tau_2) / \partial \alpha] \quad (5)$$

- AB+BT-AT (early) and b) 2·BT (late). From B's modulator and A's transponder signals, it also finds AT, whence AB. It can then adjust jamming power to disrupt communications/ ranging.

- Encryption required to secure the communication links

¹³ In general, when $\sigma \gg c/f_c$, received power doubles (the numerous target scattering returns' vector sum constituting σ , excepting for specular returns, where paths' phase shift is $[f_{c1} - f_{c2}] \cdot [AT + BT - AB]/c$).

¹⁴ As in the analogous speakerphone application, introduced frequency offsets may reduce noise resonance magnitude [15].

From an AJ standpoint, α gets upper bounded by the IC's PLL phase variance limit (a +ive K), i.e., solving (5.3-25 of [5])

$$[(G_0 N_0 + I_0) B_L / (\alpha_C^4 P^2)] \cdot [\alpha_C^2 P + (G_0 N_0 + I_0) B_L] \leq K \quad (6)$$

P and I_0 are CS power and spectral density respectively, N_0 the jammer plus noise spectral density, B_L the PLL's loop bandwidth and $G_0 = G(0, \alpha, \beta, \tau_1, \tau_2)$. Using the smaller of α_C and α_{LPI} , a minimum IC dynamic range is imposed. This RS/ CS system's required E_b/N_0 increases by $(1 + \bar{G})$ (compared to just a CS), but benefits are LPI, AJ and spectral efficiency.

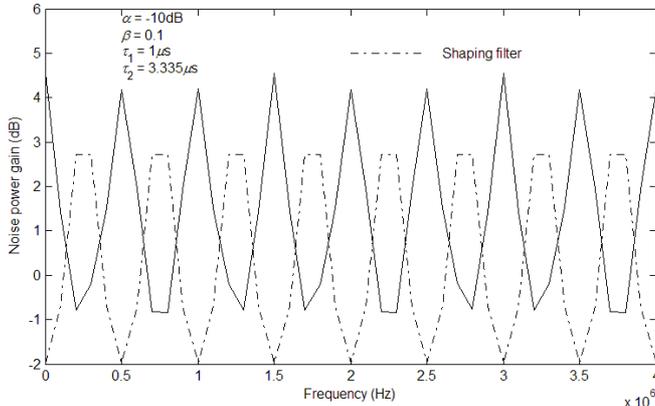


Figure 11: Example noise power gain spectrum

Kinematic-induced frequency offset does not reduce noise power (e.g., for $f_c \approx 900\text{MHz}$, 100m/s relative velocity, frequency de-coherence is 300Hz ; with 300m inter-UAV distance, phase de-coherence is just 0.024°). Though regenerative transponders avoids noise feedback, they add to demodulation/ decoding delay, in turn, requiring more stringent phase noise and low-jitter symbol timing recovery. On the other hand, the target can passively find the sum of its ranges to the UAVs, as well as the range between them, by spectral analysis (Figure 11). Range-LPI (while [16]'s dirty-paper encoding's objective and assumptions are different, its "imprecise" title is nonetheless evocative) adapts¹⁵ coding and modulation shape to UAV /target ranges, inverts partial-response at demodulator input and then decodes decision variables; when acquiring range (sweeping over B_L , in pp. 143 of [5]), unshaped modulator power is temporarily increased.

As antenna beam-widths are broad¹⁶ (and bearing information unavailable), target position is ambiguous¹⁷ to an ellipsoid (for an interceptor-pair at the two foci); Measuring range and Doppler with varying inter-foci distance, or major-axis orientation, or both, may aid disambiguation and pursuit; though beyond this paper's scope, the interceptors, during pursuit, could execute several pre-synchronized, seemingly random, ellipsoid re-orienting maneuvers (Figure 12).

¹⁵ If modulator output and IC output sample rates are in a ratio n_1/n_2 , $G(z)[1 + \alpha z^{-m}]^{-1}$ is a high-resolution shaper (for $\beta \ll \alpha \ll 1$), with $(1 + \alpha z^{-m}) \cdot G(z)$ inverting receiver partial-response, where $\alpha = \alpha/\gamma$, $\gamma =$ receiver SNR and $G(z)$ an interpolator.

¹⁶ [12]'s 1W communication antenna, a $1/4$ wave radiator on $1/4$ wave radius (8.22cm^2) ground-plane, mounts on the fuselage's top aft.

¹⁷ The last lag (of the three) is redundant (determined from the first two); disambiguation requires side information (e.g., a maneuver).

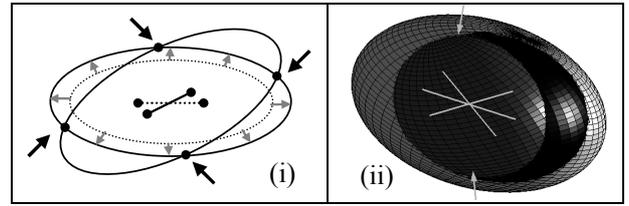


Figure 12: 2 UAVs' disambiguation by major axis rotations (i) 2-D (ii) 3-D; arrows show possible target locations

V. CONCLUSION

Conventional IC and DC systems are performance limited by system PN and these limits are derived. Ranging, inherent to IC, may also aid direction-finding and pursuit (with application to UAV swarming).

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